

Collections of sets

collections: sets that contain other sets

$$B = \{ \{0\}, \{4, 2, 1, -1, -2, -4\}, \{3, 1, -1, -3\} \}$$

↑
#s that
divide 0

↑
#s that divide 4

↑
#s that divide 3

$$|B| = 3$$

Power sets

$\mathcal{P}(A)$ is powerset of A , set of all possible subsets of A .

$$A = \{1, 2\}$$

$$\mathcal{P}(A) = \{ \emptyset, \{1\}, \{2\}, \{1, 2\} \}$$

$$\mathcal{P}(\emptyset) = \{ \emptyset \}$$

↓
recall $\emptyset \subseteq A$ for all sets A

Partitions

base set A , we can partition it into non-overlapping subsets which cover the entire base set.

$$A = \{0, 1, 4, 5, 7\}$$

$B = \{ \{0, 1\}, \{4, 5\}, \{7\} \}$ is a partition

$\{ \{7, 4\}, \{1, 5, 0\} \}$ is also a partition

rules

(1) union of elements of partition should equal base set

(2) elements should have no overlap ($b_1 \cap b_2 = \emptyset$)

③ each element should not be \emptyset

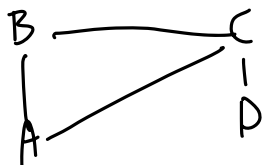
non-partitions of A

① $B = \{\{0\}, \{4,5\}, \{7\}\}$

② $B = \{\{0,1\}, \{1,4\}, \{5,7\}\}$

③ $B = \{\emptyset, \{0,1\}, \{4,5\}, \{7\}\}$

example) vertex set = $\{A, B, C, D\} = X$



$D: \mathbb{N} \rightarrow \mathbb{P}(X)$

$D(n) = \{v \in X \mid \text{degree of } v \text{ is } n\}$

$D(1) = \{D\}$

$D(2) = \{B, A\}$ ← one element of $\mathbb{P}(X)$

$S = \{D(n) \mid n \in \mathbb{N}\}$

$S = \{D(0), D(1), D(2), D(3), D(4), \dots\}$

$S = \{\emptyset, \{D\}, \{B, A\}, \{C\}, \emptyset, \dots\}$

$S = \{\emptyset, \{D\}, \{B, A\}, \{C\}\}$ ← is this a partition of X ?

no, it has the empty set as an element